## MATH 252: Elementary Differential Equations

## Quiz 2

NAME:	 Date: Sep	otember 27,	2016

Solve the following problems on this sheet of paper. **Note that there is a problem on the back.** No calculators or other electronic devices are permitted.

1. (4 points) Consider the differential equation

$$\frac{dy}{dt} = 1 + \cos y.$$

- (a) Plot the phase line for this differential equation. Hint: I suggest first plotting the right-hand side (f(y)) as a function of y.
- (b) Identify **ALL** equilibrium points as stable (sinks), unstable (sources), or semi-stable (nodes).

- 2. (2 points) Suppose we know that the function f(t,y) is continuous and that f(t,3) = -1 for all t.
  - (a) What does this tell you about the slope field for the differential equation

$$y' = f(t, y)?$$

I suggest drawing a picture, representing only the information you have been given.

(b) Suppose y(0) < 3. Is it possible that  $y(t) \to \infty$  as t increases? Give a (short) reason, using your answer from part (a). No credit will be given to simple yes/no answers.

3. (4 points) Consider the IVP

$$\begin{cases} \frac{dy}{dt} &= y^3 \\ y(0) &= 1. \end{cases}$$

- (a) Find a formula for the solution.
- (b) State the domain of definition of the solution.
- (c) What happens to the solution as it approaches the limits of its domain of definition?